

	Space with Time	
Measure of motion	<i>Time speed</i> $v_t = ds/dt \sim \ell^{-1}$	<i>Space speed</i> $v_s \Leftarrow \ell^{-1} = (dt/ds)^{-1}$
Mean speed	<i>Time mean speed</i> ($\Sigma v_i/n$)	<i>Space mean speed</i> ($\Sigma \ell_i/n$) ⁻¹
Normalized speed	$\beta = v/c \sim (\ell/k)^{-1}$	$\beta \cong (\ell/k)^{-1} \sim (v/c)$
Conversion & Lorentz factors Time-length matrix	$ct = x$ $\gamma = 1/\sqrt{1-\beta^2}$	$\begin{pmatrix} \gamma & 0 \\ 0 & 1/\gamma \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$
Galilean transformations	$\begin{pmatrix} 1 & 0 \\ -v & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	$\begin{pmatrix} 1 & -v/c^2 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$
Normalized GTs	$\begin{pmatrix} 1 & 0 \\ -\beta c & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	$\begin{pmatrix} 1 & -\beta/c \\ 0 & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$
Standard GTs	$\begin{pmatrix} 1 & 0 \\ -\beta & 1 \end{pmatrix} \begin{pmatrix} ct \\ x \end{pmatrix} = \begin{pmatrix} ct' \\ x' \end{pmatrix}$	$\begin{pmatrix} 1 & -\beta \\ 0 & 1 \end{pmatrix} \begin{pmatrix} ct \\ x \end{pmatrix} = \begin{pmatrix} ct' \\ x' \end{pmatrix}$
Lorentz transformation	$\begin{pmatrix} \gamma & -\gamma v/c^2 \\ -\gamma v & \gamma \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	
Normalized LT	$\begin{pmatrix} \gamma & -\beta\gamma/c \\ -\beta\gamma c & \gamma \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	
Symmetric LT	$\begin{pmatrix} \gamma & -\beta\gamma \\ -\beta\gamma & \gamma \end{pmatrix} \begin{pmatrix} ct \\ x \end{pmatrix} = \begin{pmatrix} ct' \\ x' \end{pmatrix}$	

	Time with Space	
Measure of motion	<i>Time pace</i> $\ell_t \Leftarrow v^{-1} = (ds/dt)^{-1}$	<i>Space pace</i> $\ell_s = dt/ds \sim v^{-1}$
Mean pace	<i>Time mean pace</i> ($\Sigma v_i/n$) ⁻¹	<i>Space mean pace</i> ($\Sigma \ell_i/n$)
Normalized pace	$\beta^{-1} = (v/c)^{-1} \sim \ell/k$	$\beta^{-1} = \ell/k \sim (v/c)^{-1}$
Conversion & Lorentz factors Length-time matrix	$\begin{pmatrix} \gamma & 0 \\ 0 & 1/\gamma \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	$kx = t$ $-\beta\gamma = 1/\sqrt{1-\beta^{-2}}$
Galilean transformations	$\begin{pmatrix} 1 & 0 \\ -k^2/\ell & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	$\begin{pmatrix} 1 & -1/\ell \\ 0 & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$
Normalized GTs	$\begin{pmatrix} 1 & 0 \\ -\beta k & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	$\begin{pmatrix} 1 & -\beta/k \\ 0 & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$
Standard GTs	$\begin{pmatrix} 1 & 0 \\ -\beta & 1 \end{pmatrix} \begin{pmatrix} t \\ kx \end{pmatrix} = \begin{pmatrix} t' \\ kx' \end{pmatrix}$	$\begin{pmatrix} 1 & -\beta \\ 0 & 1 \end{pmatrix} \begin{pmatrix} t \\ kx \end{pmatrix} = \begin{pmatrix} t' \\ kx' \end{pmatrix}$
Lorentz transformation	$\begin{pmatrix} \beta\gamma\ell & -\beta\gamma k \\ -\beta\gamma & \beta\gamma\ell/k \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	
Lorentz transformation	$\begin{pmatrix} \gamma & -\gamma/\ell \\ -\gamma k^2/\ell & \gamma \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	
Normalized LT	$\begin{pmatrix} \gamma & -\beta\gamma/k \\ -\beta\gamma k & \gamma \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$	
Symmetric LT	$\begin{pmatrix} \gamma & -\beta\gamma \\ -\beta\gamma & \gamma \end{pmatrix} \begin{pmatrix} t \\ kx \end{pmatrix} = \begin{pmatrix} t' \\ kx' \end{pmatrix}$	

